

Level Set Method for Tip Shape Evolution Simulation for Atom Probe Tomography

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Invented in 1967¹, atom probe tomography (APT) was designed to visualize chemical heterogeneity present in a small volume of a specimen with a sub-nanometer spatial resolution²⁻⁵. Numerical simulation plays an important role in studying the sample geometry evolution and corresponding electrical field changes during field evaporation of needle shaped specimens in APT. The level set method can provide sub-grid accuracy on tracking the solid-vacuum interface and much higher computational efficiency than other models that require an atomic level grid. The modeling details are introduced in our previous work⁶. The proposed approach is applied to predict the tip evaporation of the specimen, which is (100) chromium (Cr) single crystalline thin film grown on a (100) single crystalline magnesium oxide (MgO) substrate. Through comparison with experimental observation, the level set method shows the capability of providing atomic level accuracy while using a relatively coarse simulation grid that is about 5 times the atomic cell. This leads to a huge advantage in computational efficiency. The scanning transmission electron microscopy (STEM) image of the tip geometry before and after evaporation is shown in Fig. 1(a), and the comparison between STEM image and simulation results is shown in Fig. 1(b).

Additionally level set simulations were used to investigate the dynamic tip shape evolution of oxide multilayer materials. Due to their interesting interfacial properties oxide multilayered structures have acquired a lot of attention in several scientific and industrial fields, such as magnetic storage media and microelectronics. The dynamic tip shape evolution of a composite material consisting of alternating layers of CeO₂ and ZrO₂ in two orientations (top-down and side-ways) was studied by the numerical simulations. In order to study how the sample geometry and electrical field changes affect the species density distribution on the detector, a trajectory simulation model by Runge-Kutta method is integrated into the level set solid-vacuum interface tracking model. Because the grid size of the level set method is around 5 times the atomic volume, a local grid refinement method is used for initialization of the starting positions of evaporated atoms for the trajectory calculation. Fig. 2 shows the simulation results for the CeO₂ and ZrO₂ horizontal multilayer sample evaporation. Fig. 2(a) and (b) show the tip geometry and electric field evolution during evaporation after 0 and 5000 atoms are evaporated respectively. Fig. 2(c) shows the end position of atoms flying over the counter electrode, and Fig. 2(d) shows the atom density distribution on the selected region as shown on Fig. 2(c). Because the evaporation strength of ZrO₂ is about double that of CeO₂, CeO₂ is evaporated much faster and easier than ZrO₂, which causes concaves for CeO₂ on the tip surface. The concaves on the tip surface lead to higher density of electrical field lines, and make the trajectories of Ce closer to each other. This is consistent with the narrower band of Ce and wider band of Zr in the density distribution as shown in Fig. 2(d), which is fairly well matched to the experiment observations and measurements. Similarly, Fig. 3 shows the simulation results for the CeO₂ and ZrO₂ vertical multilayer sample evaporation.

Reference

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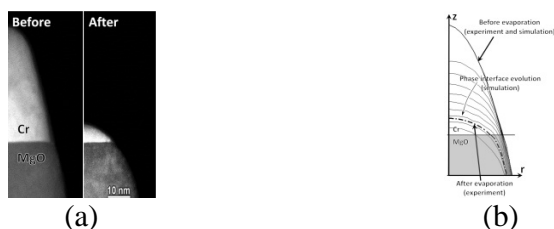


Fig. 1: (a) scanning transmission electron microscopy (STEM) side view of the tested specimen before and after evaporation, (b) Comparison between the simulation results and the observation of the experiment.

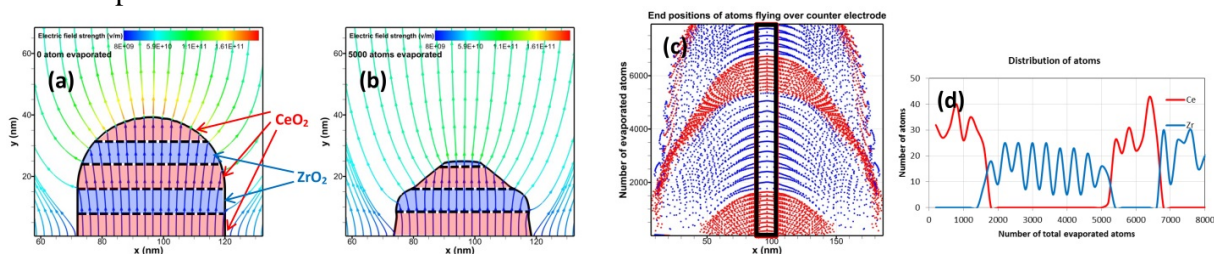


Fig. 2: Simulation results for the CeO_2 and ZrO_2 horizontal multilayer sample evaporation; (a) and (b): the tip geometry and electric field evolution during evaporation after 0 and 5000 atoms are evaporated respectively; (c): end position of atoms flying over counter electrode; (d): atoms density distribution on the selected region as shown on (c).

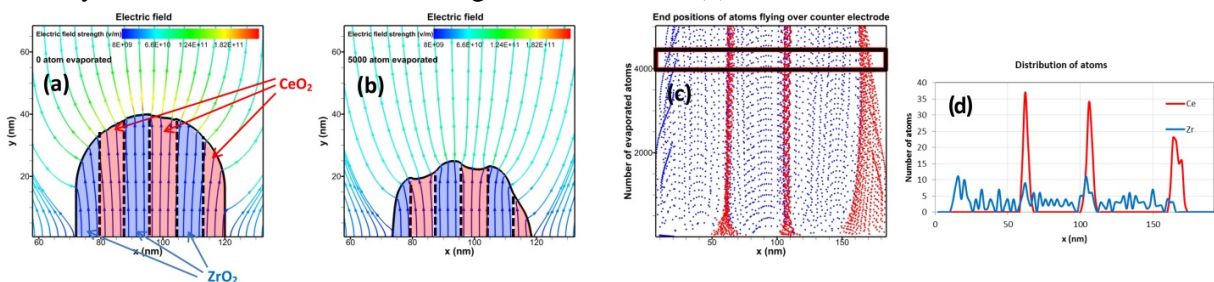


Fig. 3: Simulation results for the CeO_2 and ZrO_2 vertical multilayer sample evaporation; (a) and (b): the tip geometry and electric field evolution during evaporation after 0 and 5000 atoms are evaporated respectively; (c): end position of atoms flying over counter electrode; (d): atoms density distribution on the selected region as shown on (c).