

# Energetics of gating at the apo-acetylcholine receptor transmitter binding site

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Acetylcholine receptor channels switch between conformations that have a low versus high affinity for the transmitter and conductance for ions ( $R \leftrightarrow R^*$ ; gating). The forward isomerization, which begins at the transmitter binding sites and propagates  $\sim 50$  Å to the narrow region of the pore, occurs by approximately the same sequence of molecular events with or without agonists present at the binding sites. To pinpoint the forces that govern the R versus  $R^*$  agonist affinity ratio, we measured single-channel activation parameters for apo-receptors having combinations of mutations of 10 transmitter binding site residues in the  $\alpha$  (Y93, G147, W149, G153, Y190, C192, and Y198),  $\epsilon$  (W55 and P121), or  $\delta$  (W57) subunit. Gating energy changes were largest for the tryptophan residues. The  $\alpha$ W149 energy changes were coupled with those of the other aromatic amino acids. Mutating the aromatic residues to Phe reduces the  $R/R^*$  equilibrium dissociation constant ratio, with  $\alpha$ Y190 and  $\alpha$ W149 being the most sensitive positions. Most of the mutations eliminated long-lived spontaneous openings. The results provide a foundation for understanding how ligands trigger protein conformational change.

## INTRODUCTION

The neuromuscular acetylcholine (ACh) receptor (AChR) is an allosteric protein in which a change in affinity for ACh at two transmitter binding sites is coupled with a global gating conformational change that regulates ionic conductance (Edelstein and Changeux, 1998; Karlin, 2002; Lester et al., 2004; Sine and Engel, 2006; Auerbach, 2010). In the absence of agonists, wild-type (wt) AChRs rarely switch from the nonconducting R shape to the ion-conducting  $R^*$  shape, but, after binding two transmitter molecules, the probability of this occurring increases dramatically.

The magnitude of the diliganded gating equilibrium constant ( $E_2$ ) is the product of two fundamental parameters: the intrinsic tendency of the protein to isomerize spontaneously (the unliganded gating equilibrium constant,  $E_0$ ) and the change in affinity for agonists at each of the two transmitter binding sites (the  $R/R^*$  equilibrium dissociation constant ratio,  $K_d/J_d$ ; Fig. 1). In adult mouse wt neuromuscular AChRs activated by ACh ( $-100$  mV at  $23^\circ\text{C}$ ),  $E_2 = \sim 28$  (Chakrapani et al., 2003), which is the product of  $E_0 (= \sim 6.5 \times 10^{-7})$  times  $(K_d/J_d)^2 (= \sim 6,600)^2$  (Jha and Auerbach, 2010). From the natural logarithm of  $(K_d/J_d)$ , we estimate that each of the two ACh molecules is more stably bound to  $R^*$  versus R by  $\sim 5.2$  kcal/mol.

It is of interest to pinpoint and characterize the molecular forces that underlie the difference in ACh binding energy, R versus  $R^*$ . Each AChR transmitter binding site has five aromatic residues that are important to both ligand binding and channel gating (Fig. 2). With ACh as

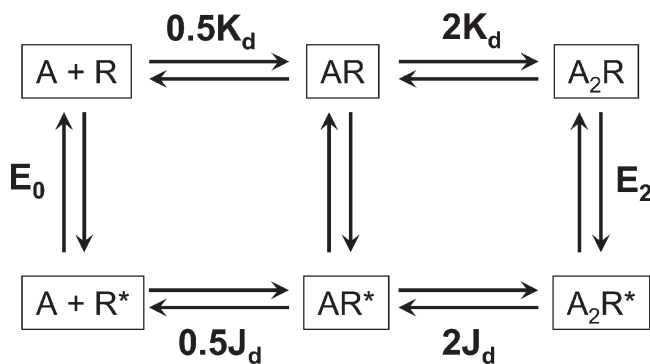
the agonist, point mutations of these positions increase  $K_d$  and decrease  $E_2$  (Aylwin and White, 1994; O'Leary et al., 1994; Sine et al., 1994; Chen et al., 1995; Akk et al., 1996, 1999; Chiara et al., 1998; Akk, 2001; Bafna et al., 2009). It has been difficult to probe in detail the role of these aromatic residues because their mutation can reduce the affinity for agonists to such a degree that measuring currents from diliganded AChRs becomes impossible. As a consequence, the extent to which mutations of these residues change  $E_0$  versus  $K_d/J_d$  is unknown. It is possible, however, to quantify the gating energy changes experienced by these residues in mutant AChRs that spontaneously undergo the  $R \leftrightarrow R^*$  isomerization in the absence of exogenous ligands (Purohit and Auerbach, 2009). Probing the binding site residues in apo-AChRs not only reveals their energy contributions to binding and gating but is also likely to reflect their behaviors in the presence of agonists because the mechanism of gating is approximately the same with and without ligands (Purohit and Auerbach, 2009). In this study, we estimate  $E_0$  for 123 different mutations of 10 different amino acids at the adult mouse neuromuscular AChR transmitter binding sites.

## MATERIALS AND METHODS

Mutants were made by using the QuikChange Site-Directed Mutagenesis kit (Agilent Technologies) and were confirmed by complete cDNA sequencing. Human embryonic kidney 293 cells were

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Abbreviations used in this paper: ACh, acetylcholine; AChBP, ACh-binding protein; AChR, ACh receptor; wt, wild type.



**Figure 1.** Cyclic scheme for AChR activation. Stable conformations are boxed, equilibrium constants are bold, and transient intermediate states are represented by arrows. R, conformation with a low affinity for agonists and a nonconducting channel; R\*, conformation with a high affinity for agonists and a conducting channel; A, the agonist. The two binding sites are equivalent.  $K_d$  and  $J_d$  are the equilibrium dissociation constants from R and R\*.  $E_0$  and  $E_2$  are the gating equilibrium constants for the apo- and diliganded protein. The energy difference between any two stable states is independent of the connecting pathway, so  $E_2/K_d^2 = E_0/J_d^2$  or  $E_2 = E_0(K_d/J_d)^2$ .

transiently transfected using calcium phosphate precipitation with a mixture of cDNAs encoding mouse muscle AChRs ( $\alpha$ ,  $\beta$ ,  $\delta$ , and  $\epsilon$ ;  $\sim 3\text{--}4\ \mu\text{g}/35\text{-mm}$  dish in a 2:1:1:1 ratio).  $0.1\ \mu\text{g}/\mu\text{l}$  cDNA encoding green fluorescent protein was added as a marker to the transfection cocktail. The cells were incubated at  $37^\circ\text{C}$ ; the culture medium was washed after  $\sim 16$  h, and single-channel patch clamp recording was performed in the cell-attached configuration (Hamill et al., 1981)  $\sim 4\text{--}6$  h later at  $23^\circ\text{C}$ . Currents were sampled at 50 kHz after low-pass filtering at 20 kHz. QuB software (State University of New York at Buffalo) was used to acquire and analyze the single-channel currents.

The bath solution was Dulbecco's phosphate-buffered saline containing 137 mM NaCl, 0.9 mM  $\text{CaCl}_2$ , 2.7 mM KCl, 1.5 mM  $\text{KH}_2\text{PO}_4$ , 0.5 mM  $\text{MgCl}_2$ , and 8.1 mM  $\text{Na}_2\text{HPO}_4$ , pH 7.4. The pipette solution was the same as the bath, and the pipette potential was 70 mV, which corresponds to a membrane potential ( $V_m$ ) of approximately  $-100$  mV. The pipette solution contained no added agonist, and the pipette holder/electrodes were never exposed to an AChR agonist.

In wt AChRs, unliganded openings are both rare and brief. To increase both the frequency and duration of such openings, we used a background construct that had multiple point mutations in both  $\alpha$  subunits: ( $\alpha\text{D97A}+\alpha\text{Y127F}+\alpha\text{S269I}$  [DYS]). Individually, each of these mutations increases the diliganded gating equilibrium constant ( $E_2$ ;  $\alpha\text{D97A}$ , 168-fold [Chakrapani et al., 2003];  $\alpha\text{Y127F}$ , 59-fold [Purohit and Auerbach, 2007];  $\alpha\text{S269I}$ , 115-fold [Mitra et al., 2005]) by an approximately parallel change in the unliganded gating equilibrium constant ( $E_0$ ; Purohit and Auerbach, 2009). None of the mutations had a measurable effect on  $K_d$ . If the energetic consequence of each mutation is independent of the others, we estimate that the net increase in  $E_0$  in this background is  $168 \times 59 \times 115 = 1.10^6$ . The fold changes in  $E_0$  of the binding site mutations in this study are expressed in reference to the DYS background, so the only assumption we make is that the binding site and DYS mutations (combined) have independent energetic consequences. Expression was robust for most mutant constructs. Because there was no ACh in the pipette solution, there was no agonist-associated open-channel block, and the single-channel current amplitude was in all cases  $\sim 7$  pA.

We define  $E_0$  as the  $R \leftrightarrow R^*$  isomerization equilibrium constant in the absence of exogenous agonist molecules and under the aforementioned experimental conditions. A mutation that changes  $E_0$  changes the relative free energy difference between the R and R\* shapes of the apo-AChR. This energy difference could be generated by altered interactions between any or all of the structural elements that comprise the apo-AChR transmitter binding site, including the protein, water molecules, and ions.

QuB software was used to acquire and analyze the single-channel currents. The raw data were corrected for baseline drift. Clusters of single-channel openings were then selected by eye, and the currents were idealized into noise-free conducting/nonconducting intervals by using a segmental k-means algorithm (Qin, 2004). To estimate unliganded opening ( $f_0$ ) and closing ( $b_0$ ) rate constants, the idealized current intervals were modeled using the maximum interval likelihood method after imposing a 25- $\mu\text{s}$  dead time and missed event correction (Qin et al., 1997).

The fold change in  $E_0$  ( $= f_0/b_0$ ) for each mutant was estimated as  $E_0^{\text{mutant}}/E_0^{\text{DYS}}$ . The change in the free energy ( $\Delta\Delta G$ ) as a result of mutation was estimated as  $\Delta\Delta G$  (kilocalories/mole)  $= -0.59$  natural logarithm ( $\ln$ ;  $E_0^{\text{mutant}}/E_0^{\text{DYS}}$ ). The coupling energy between side chains was calculated as  $\Delta\Delta G$  (kilocalories/mole)  $= -0.59 \ln$  (observed  $E_0^{\text{mutant}}/\text{predicted } E_0^{\text{mutant}}$ ). The predicted value was calculated as the sum of the  $\Delta\Delta G$  values for each individual mutation.

In almost all of the binding site mutants (94%; 104 of 111 constructs on the DYS background), the spontaneous open- and closed-interval durations were described by a single exponential component. For these,  $f_0$  and  $b_0$  were the inverse mean lifetime of the nonconducting and conducting intervals. For the remaining constructs (wt,  $\alpha\text{Y93G}$ ,  $\alpha\text{Y190G}$ ,  $\alpha\text{G153S}$ , and  $\epsilon/\delta\text{W55/57 R}$  and E), both brief ( $\sim 0.25$  ms) and long ( $\sim 1.0$  ms) open-interval components were apparent. For these constructs, interval durations were fitted by a kinetic model having two nonconducting and two conducting states. We tested both the COOC and OCCO kinetic schemes, with nearly equivalent results for the  $E_0$  estimate. The values reported in the tables were obtained by using the first model, with  $E_0$  calculated as the ratio of  $f_0/b_0$  associated with the predominant ( $\sim 90\%$ ), brief component.

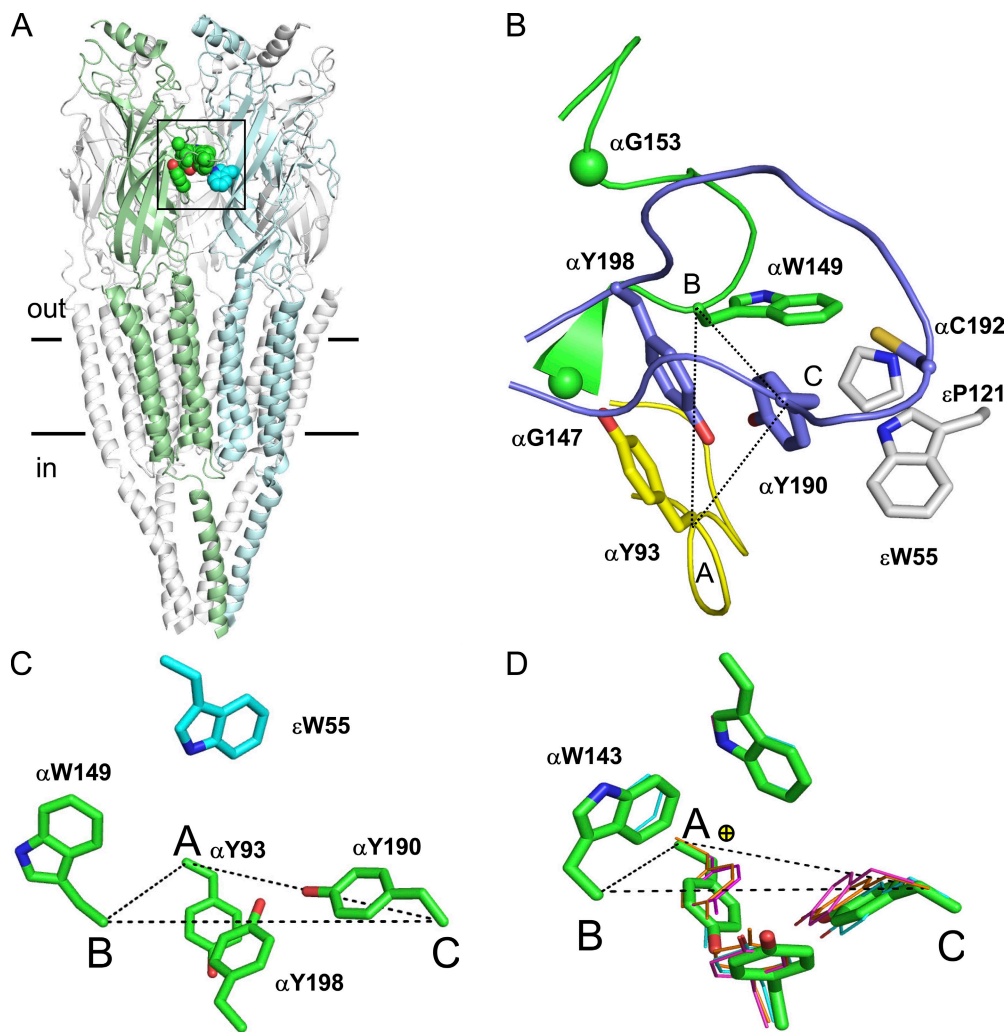
We define a range energy value as the natural logarithm of the ratio of the largest/smallest  $E_0$  value for a series of mutations of one position (Jha et al., 2009). This parameter is a minimum estimate of the sensitivity of a position to perturbation in  $R \leftrightarrow R^*$  gating. The interaction energy between residues was determined for a handful of side chain substitutions of each pair. The maximum observed interaction energy (the coupling range energy) is a minimum estimate of the extent to which side chains of the two positions can be coupled energetically. Additional mutations (both natural and unnatural) may increase the range energy and coupling range energy estimates.  $\Phi$  is the unweighted, straight-line slope of the rate equilibrium (R/E) plot, which is  $f_0$  versus  $E_0$  on a log-log scale.

#### Online supplemental material

Figs. S1–S5 show example clusters and coupling energy estimates for transmitter binding site aromatic mutant pairs. The rate and equilibrium constants are given in Tables S1–S6. Online supplemental material is available at <http://www.jgp.org/cgi/content/full/jgp.200910384/DC1>.

## RESULTS

The unliganded *Torpedo* AChR structure is shown in Fig. 2. The two transmitter binding sites are in the extracellular domain of the  $\alpha$  subunit, close to the interface with the  $\epsilon$  or  $\delta$  subunit. Each binding site has



**Figure 2.** The AChR transmitter binding site. (A) Unliganded *Torpedo* AChR (2bg.pdb9; Unwin, 2005).  $\alpha$  subunit, green;  $\epsilon$  subunit, light blue. The binding site aromatic residues are shown as spheres (horizontal lines, membrane). (B) Close-up of the  $\alpha$ - $\epsilon$  transmitter binding site (boxed area in A) showing the salient residues in loop A (yellow), loop B (green), loop C (purple), and the  $\epsilon$  subunit (gray; O, red; N, blue; S, yellow).  $\alpha$ G147 and  $\alpha$ G153 C $\alpha$  atoms are spheres. Dotted lines connect C $\alpha$  atoms from  $\alpha$ Y93 (loop A),  $\alpha$ W149 (loop B), and  $\alpha$ Y190 (loop C). (C) In the AChR,  $\alpha$ W149 and  $\epsilon$ W55 are spread. (D) In AChBP, the two tryptophans are edge to face in apo- and all liganded structures. No ligand, green (1UV6.pdb; Celie et al., 2004); nicotine, magenta (1UW6.pdb; Celie et al., 2004); carbamylcholine, orange (1UV6.pdb; Celie et al., 2004); and HEPES, cyan (1I9B.pdb; Brejc et al., 2001). Yellow sphere, quaternary amine of carbamylcholine.

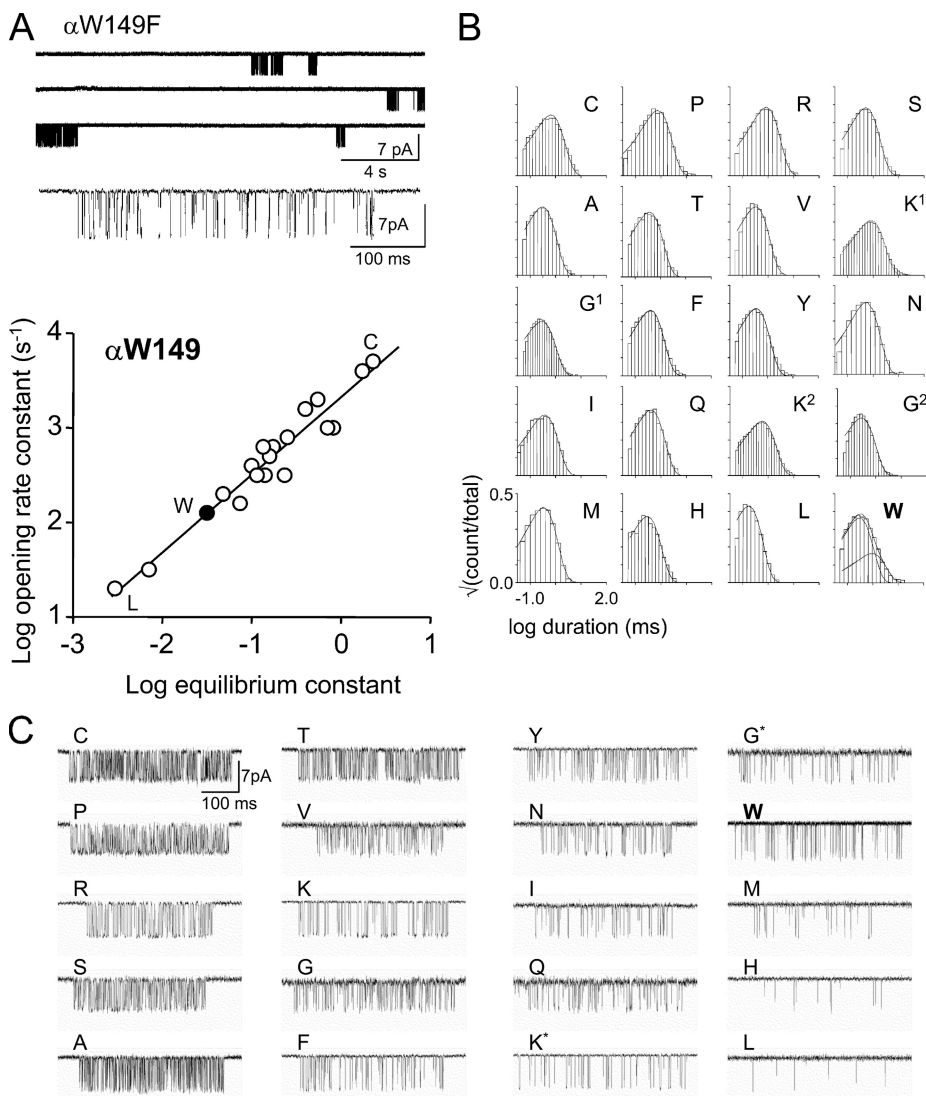
several conserved aromatic side chains, namely Y93 (loop A), W149 (loop B), Y190 and Y198 (loop C) in the  $\alpha$  subunit (the primary side of the binding site), and W57/55 in the adjacent  $\delta$ / $\epsilon$  subunit (the complementary side; strand  $\beta_2$ ). The nonaromatic binding site residues we investigated are  $\alpha$ G147 and  $\alpha$ G153 (loop B),  $\alpha$ C192 (loop C), and  $\epsilon$ P121 (between strands  $\beta_6$  and  $\beta_6'$ ).

#### Point mutations of aromatic residues

Position  $\alpha$ W149 was mutated to all 19 natural side chains (Fig. 3). These mutants were expressed on a high gain of function background construct ( $\alpha$ D97A+ $\alpha$ Y127F+ $\alpha$ S269I [DYS]). This combination of mutations increases the unliganded gating equilibrium constant  $E_0$  about a million-fold but does not affect  $K_d$  for ACh, the  $K_d/J_d$  affinity ratio for ACh, or the gating conformational pathway. In this construct, spontaneous  $R \leftrightarrow R^*$  gating intervals arising from individual apo-AChRs occur in clusters (Fig. 3 A, top; Purohit and Auerbach, 2009). We assumed that the fold changes in  $E_0$  caused by the  $\alpha$ W149 mutations on the DYS

background are the same as would have occurred on the wt background.

We were unable to record single-channel currents from cells transfected with the  $\alpha$ W149D or  $\alpha$ W149E mutants either because of low expression in the cell membrane or because the probability of observing openings was extremely low. AChRs having 1 of the 17 remaining mutant side chains produced clustered openings from which we could estimate the single-channel, unliganded  $R \rightarrow R^*$  ( $f_0$ ) and  $R \leftarrow R^*$  ( $b_0$ ) rate constants and the corresponding reaction equilibrium constant ( $E_0 = f_0/b_0$ ). Furthermore, because we know these values for the background construct alone, we can calculate the fold changes in  $f_0$  and  $E_0$  caused specifically by each  $\alpha$ W149 side chain substitution (Table S1). AChRs with wt transmitter binding sites that are active spontaneously show both brief and long components in the open-interval duration histograms (Jackson, 1984, 1986; Grosman and Auerbach, 2000; Grosman, 2003; Purohit and Auerbach, 2009). All 17 of the  $\alpha$ W149 mutations completely eliminated the long open component (Fig. 3 B).



**Figure 3.** Mutations of  $\alpha$ W149. (A) Spontaneous currents from  $\alpha$ W149F (conducting is down; DYS background). (top) Long gaps between clusters are epochs when all of the AChRs in the patch are in states associated with desensitization. (middle) A cluster at higher resolution. The closed and open intervals reflect unliganded  $R \leftrightarrow R^*$  gating. (bottom) Rate equilibrium (R/E) plot for  $\alpha$ W149. Solid circle, wt. Most mutations increased the spontaneous gating equilibrium constant ( $E_0$ ) relative to the wt. The ratio of the largest (Cys) to smallest (Leu)  $E_0$  value represents an energy difference of 4.0 kcal/mol. (B) Open-interval duration histograms. All side chains except W have a single open-interval component. (C) Example of unliganded clusters from  $\alpha$ W149 mutants (low-pass filtered to 2 kHz; Asp and Glu substitutions did not yield functional AChRs). Only the Gly and Lys mutations showed two distinct kinetic forms (marked by asterisks).

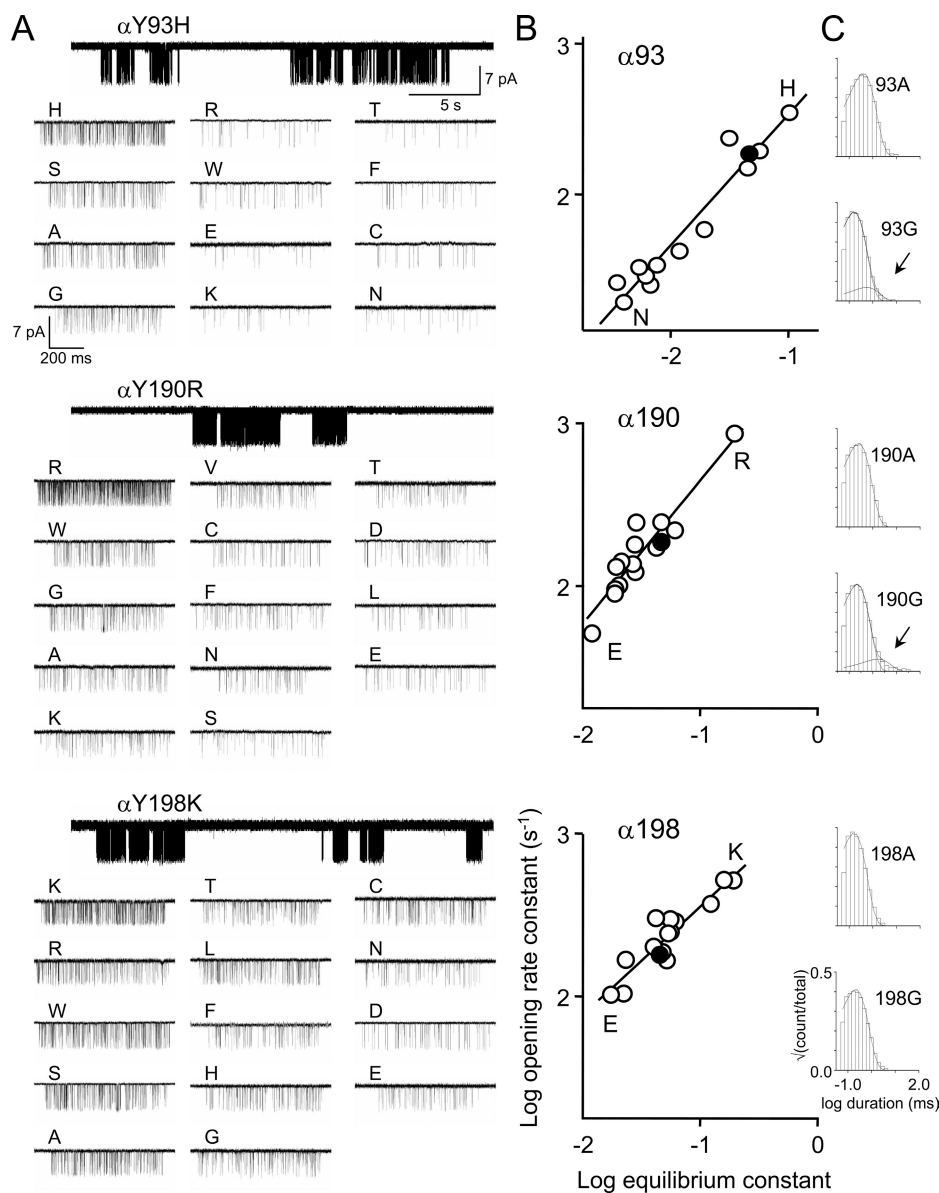
Most of the  $\alpha$ W149 mutants increased  $E_0$  and, thus, the probability of adopting  $R^*$ . This indicates that AChRs bearing these side chains are more energetically stable in  $R^*$  versus  $R$  compared with the wt. The three exceptions were Met, His, and Leu, which were modestly less stable in  $R^*$ . Equilibrium constants are functions of the free energy difference between  $R$  and  $R^*$ , and from our measurements we cannot determine the extent to which the changes in  $E_0$  specifically arose from changes in the stability of either end state conformation.

We define the energy difference between the smallest and largest values of  $E_0$  for a series of mutations of one position as the range energy, which is a minimum estimate of the energy sensitivity of that position in the  $R \leftrightarrow R^*$  isomerization (Jha et al., 2009). The largest fold increase in  $E_0$  at  $\alpha$ W149 was with a Cys substitution ( $\sim 53$ -fold), and the largest fold decrease was with a Leu substitution ( $\sim 17$ -fold). Thus, an L to C substitution at position  $\alpha$ W149 causes an  $\sim 885$ -fold change in  $E_0$ , and

the  $\alpha$ W149 range energy (for both  $\alpha$  subunits combined) is  $\sim 4.0$  kcal/mol.

The results for the  $\alpha$ W149 mutants are summarized in the form of a rate equilibrium (R/E) plot in Fig. 3 A. The slope of this relationship,  $\Phi$ , is a number between one and zero that reflects the relative timing (early to late) of the energy change experienced by the perturbed side chain between its structures in  $R$  versus  $R^*$  (Auerbach, 2005; Zhou et al., 2005). The high  $\Phi$  value for position  $\alpha$ W149 ( $0.82 \pm 0.04$ ) suggests that its gating energy change occurs near the beginning of the forward isomerization process, about the same time as the energy change of the agonist molecule ( $\Phi = \sim 0.91$ ; Grosman et al., 2000).

The effects of mutating the complementary binding site Trp residues  $\epsilon$ W55 and  $\delta$ W57 have been reported previously (Akk, 2002; Bafna et al., 2009). With regard to unliganded AChRs, the range energy for each of these two positions was 1.1 kcal/mol (W to H) and 1.7 kcal/mol (L to H), respectively (Bafna et al., 2009).



**Figure 4.** Mutations of  $\alpha Y93$ ,  $\alpha Y190$ , and  $\alpha Y198$ . (A) Single-channel current traces at low (top) and high resolution. (B) Rate equilibrium plots. Filled circles, wt.  $\alpha Y93$ ,  $\alpha Y190$ , and  $\alpha Y198$  all exhibit smaller range energies (2.0 kcal/mol, 1.6 kcal/mol, and 1.4 kcal/mol, respectively) compared with  $\alpha W149$  (4.0 kcal/mol; Fig. 3 A). (C) Example of open-interval duration histograms. All construct mutants had a single open-interval component except  $\alpha Y93G$  and  $\alpha Y190G$ . Arrows indicate longer open components.

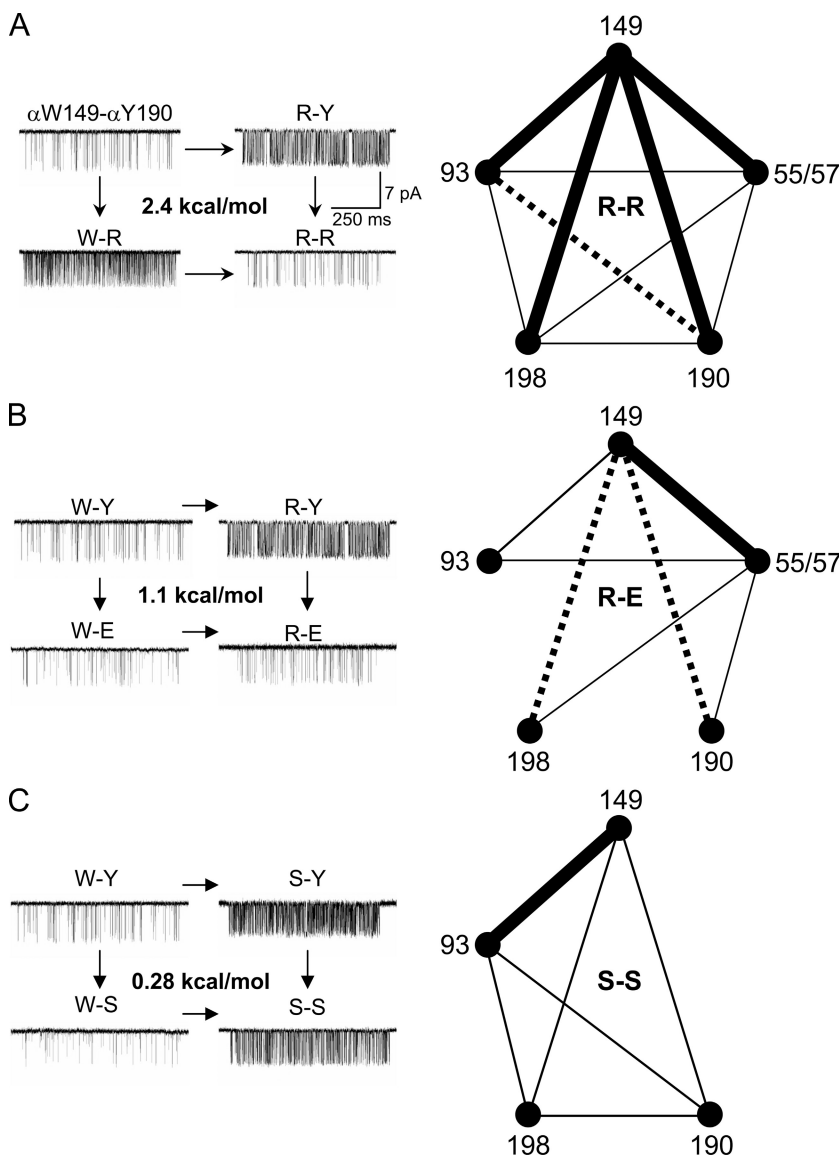
To compare these energies with those from the  $\alpha$ -subunit side (for which there are two mutations per AChR), we estimated the degree of energy coupling between  $\epsilon W55$  and  $\delta W57$ . The sums of the energy changes for the Glu or Arg individual mutations of the two complementary tryptophans were similar to those observed in the double mutants, indicating that the energetic consequences of the mutations are approximately independent (Fig. S5 and Table S4). We estimate that the range energy for  $\epsilon W55$  and  $\delta W57$  combined ( $\epsilon H + \delta H$  to  $\epsilon W + \delta L$ ) is  $\sim 2.8$  kcal/mol.

We performed similar analyses of unliganded gating for mutations of the three tyrosine residues  $\alpha Y93$ ,  $\alpha Y190$ , and  $\alpha Y198$  (Fig. 4 and Table S2). At these positions, Asp and Glu substitutions produced functional AChRs that had a reduced  $E_0$ , except for the  $\alpha Y93D$  construct, for which no currents were observed. The

range energy values for these three positions were 2.0 kcal/mol, 1.6 kcal/mol, and 1.4 kcal/mol, respectively, all smaller than for each of the two tryptophan positions. The slopes of the R/E plots for  $\alpha Y93$ ,  $\alpha Y190$ , and  $\alpha Y198$  were  $0.86 \pm 0.06$ ,  $0.88 \pm 0.09$ , and  $0.66 \pm 0.06$ , respectively. In 95% (38 of 40) of the Tyr mutations, only a single spontaneous open time component was apparent. Histograms from the two exceptions,  $\alpha Y93G$  and  $\alpha Y190G$ , are shown in Fig. 4 C.

#### Pairwise mutations of aromatic residues

In the next set of experiments, we measured the extent to which the energy changes in the aromatic residues are independent of each other (Fig. 5, Figs. S1 and S2, and Tables S3 and S4; Horowitz and Fersht, 1990). First,  $\alpha W149$  was mutated in combination with side chain substitutions  $\alpha Y190$ ,  $\alpha Y198$ , or  $\alpha Y93$ . Six different pairs



**Figure 5.** Energy coupling between aromatic residues. (A–C, left) Example of clusters for  $\alpha$ W149– $\alpha$ Y190 mutant pairs. (A–C, right) Coupling diagrams (thick lines, >2 kcal/mol; dashed lines, 1–2 kcal/mol; thin lines, <1 kcal/mol; no line, interaction not studied). (A) R–R substitutions. (left) An R mutation at  $\alpha$ 149 or  $\alpha$ 190 increases  $E_0$ , but both R mutations reduce  $E_0$  (coupling energy, 2.4 kcal/mol). (right) With R substitutions, all aromatic residues are coupled to  $\alpha$ W149 by >2 kcal/mol. (B) R–E substitutions.  $\alpha$ W149 interactions are strongest with  $\epsilon$ 55( $\delta$ 57) and nil with  $\alpha$ Y93. (C) S–S substitutions. The only strong interaction is between  $\alpha$ 149 and  $\alpha$ 93 (Figs. S1–S5 and Tables S3 and S4).

of side chains were probed to estimate the 149–190 interaction (coupling) energy (Y–W, S–S, A–A, R–D, R–E, and R–R). When both 149 and 190 were mutated to Arg, the observed  $E_0$  was substantially smaller than predicted from independence (Fig. 5 A, left). This R–R combination exhibited 2.4 kcal/mol (unfavorable) interaction energy. When the side chains at these two positions were swapped (Y–W), or with the R–D or R–E pairs, the combined effect showed an intermediate,  $\sim$ 1.1 kcal/mol deviation from independence (Fig. 5 B, left). When both residues were mutated to Ser or Ala (Fig. S1 A), the observed  $E_0$  was very close to that predicted from independent action (Fig. 5 C, left).

The coupling patterns for 149–198 and 149–93 mutant pairs were similar, but not identical, to that for 149–190 (Table S3). The R–R substitutions for all three pairs showed a similarly high degree of coupling,  $\sim$ 2.4 kcal/mol. The R–D pairs also were similarly coupled at

149–190 and 149–198 (1.1 kcal/mol). The A–A pairs showed no (149–198,  $-0.2$  kcal/mol) or some (149–93,  $0.8$  kcal/mol) energetic coupling. The 149–93 R–E pair behaved approximately independently, whereas this combination at 149–198 and 149–190 showed some coupling (1.5 kcal/mol and 1.1 kcal/mol, respectively). Although S–S at 149–190 and 149–198 show little or no coupling, these two side chains interact strongly (2.4 kcal/mol) in the 149–93 pair. In summary, the interaction pattern was different for 149–93 compared with 149–190 and 149–198 for three different side chain pairs (S–S, A–A, and R–E). S–S and R–R pairwise interactions between the three tyrosines are shown in Fig. S2 and Table S3. In all cases, the interaction energy was intermediate ( $\sim$ 1.3 kcal/mol) for R–R combinations.

We also measured the coupling energy between the four  $\alpha$ -subunit aromatic residues and the complementary  $\delta/\epsilon$  W57/55 (Figs. S3 and S4 and Table S4). The pairwise

interaction energies were mostly small (<1 kcal/mol). Larger interaction energies were apparent for the R–R pairs (~2.2 kcal/mol) and for the R–E pair, which was more strongly coupled at the  $\alpha$ – $\delta$  interface (2.1 kcal/mol) than at the  $\alpha$ – $\varepsilon$  interface (0.9 kcal/mol). The constructs  $\varepsilon$ W55E+ $\delta$ W57E and  $\varepsilon$ W55R+ $\delta$ W57R showed little coupling (<0.5 kcal/mol). However,  $\alpha$ W149R+ $\varepsilon$ W55E+ $\delta$ W57E showed a coupling energy of 1.4 kcal/mol. This suggests that with an R (but not a W) at position  $\alpha$ 149, the two complementary positions interact. The coupling energies for R–R, R–E, and S–S pairs are summarized in the diagrams in Fig. 5. AChRs having all four  $\alpha$ -subunit aromatic positions mutated to R (in both subunits) expressed successfully (Fig. S5).

From the pairwise mutation experiments, we conclude that at the AChR transmitter binding site (a)  $\alpha$ W149 is energetically the most strongly linked residue; (b) the degree of coupling between side chains depends on the chemical nature of the substitutions; (c) the interactions, when present, are all unfavorable (reduce  $E_0$  more than expected from independence); (d)  $\alpha$ Y93 in loop A has a different relationship with  $\alpha$ W149 compared with the two loop C Tyr residues; and (e) the AChR gating isomerization is robust, insofar as receptors having all eight binding site aromatic residues in the two  $\alpha$  subunits replaced with Arg still can isomerize between R and R\* conformations.

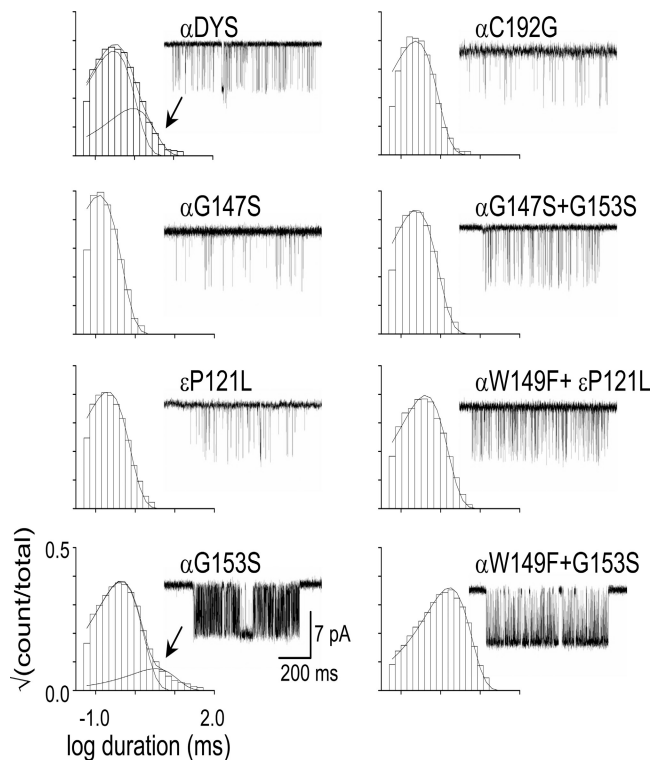
#### Mutations of nonaromatic residues

We also examined point mutations of four nonaromatic amino acids at the transmitter binding site (Fig. 6 and Table S5). Two Gly residues in loop B ( $\alpha$ G147 and  $\alpha$ G153) bracket  $\alpha$ W149 (Fig. 2). The mutation  $\alpha$ G147S produced a small (approximately eightfold) decrease in  $E_0$ , and the slow-channel congenital myasthenia mutation  $\alpha$ G153S (Sine et al., 1995) produced a moderate (~28-fold) increase in  $E_0$ . The mutation  $\alpha$ C192G (at the tip of loop C) showed a small, approximately twofold reduction in  $E_0$ . The complementary binding site mutation  $\varepsilon$ P121L, which was reported to reduce  $E_2$  by ~500-fold (Ohno et al., 1996), had no measurable effect on  $E_0$ . The mutations  $\alpha$ C192G,  $\alpha$ G147S, and  $\varepsilon$ P121L eliminated the long component of spontaneous openings, but these were still apparent in the loop B mutant  $\alpha$ G153S (Fig. 6).

We also made pairwise mutations involving some of these four positions (Table S5). The double mutant  $\alpha$ G147S+ $\alpha$ G153S reduced  $E_0$  by 1.3-fold, which translates to a modest coupling energy of 0.9 kcal/mol. The other two combinations,  $\alpha$ G153S+ $\alpha$ W149F and  $\varepsilon$ P121L+ $\alpha$ W149F, showed little energetic coupling (–0.6 kcal/mol and 0.3 kcal/mol, respectively).

#### Multiple open components

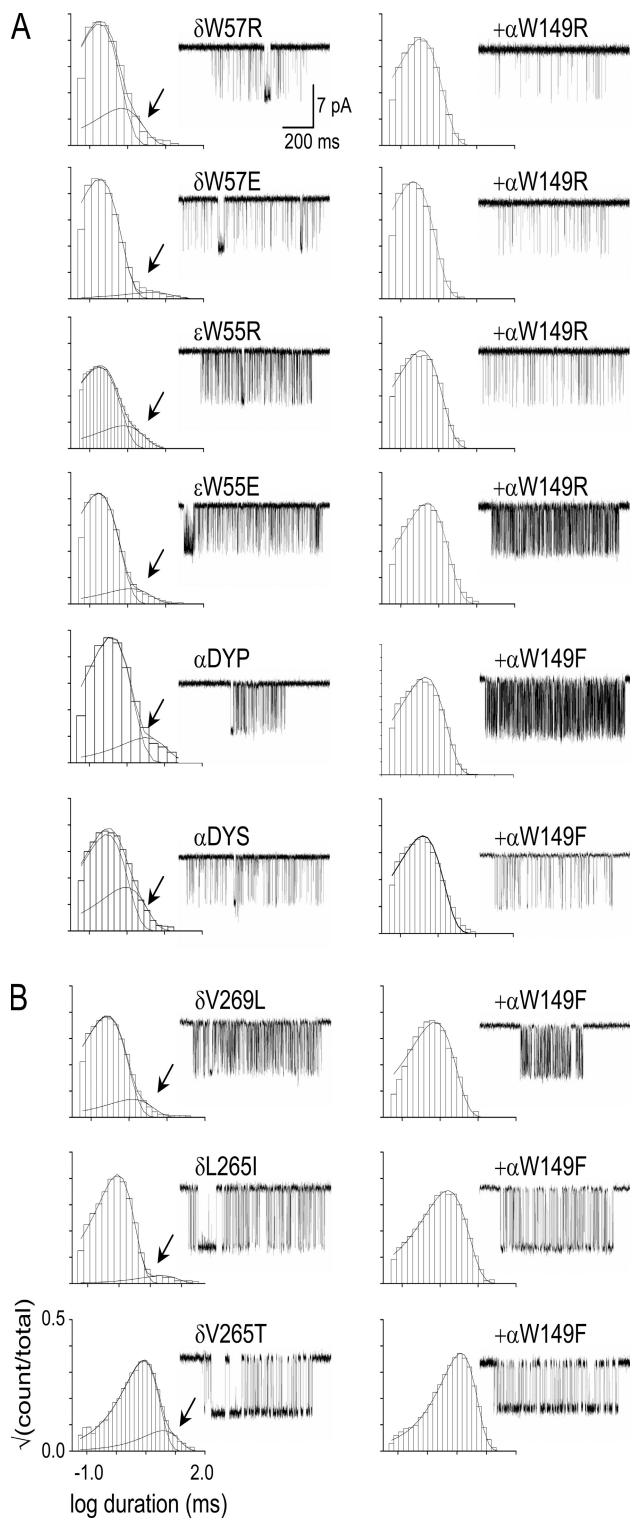
The long open-interval lifetime component was absent after 57 of 60 different  $\alpha$ -subunit binding site mutations of residues in loops A ( $\alpha$ Y93), B ( $\alpha$ G147 and  $\alpha$ W149),



**Figure 6.** Mutations of nonaromatic binding site residues. Each panel shows an open-interval duration histogram and example cluster for the indicated mutation.

and C ( $\alpha$ Y190,  $\alpha$ C192, and  $\alpha$ Y198). The three exceptions were  $\alpha$ G153S,  $\alpha$ Y190G, and  $\alpha$ Y198G. The long open component was also not apparent in  $\varepsilon$ P121L but was present after mutation of the complementary  $\varepsilon$ / $\delta$ W55/57 residues to Arg or Glu.

To explore the origin of long openings, we recorded spontaneous currents from AChRs having both an  $\alpha$ W149 side chain substitution that by itself eliminates the long openings and a secondary mutation that by itself does not. When the secondary mutation was nearby ( $\alpha$ G153S) or at the complementary side of the binding site ( $\varepsilon$ W55R/E or  $\delta$ W57R/E), the long open component vanished. When the additional mutation was at a distant position between the binding site and the gate ( $\alpha$ P272A [the M2–M3 linker; Jha et al., 2007],  $\alpha$ S269I [M2–28'; Mitra et al., 2005],  $\delta$ V269L [M2–13'; Cymes et al., 2002],  $\delta$ L265I/T [M2–9'; Cymes et al., 2002]), the long component vanished (Fig. 7 B). As shown in Fig. 7, mutation of the loop B residue  $\alpha$ W149 eliminated long openings on all 10 backgrounds on which it was examined. This pattern suggests that spontaneous and brief versus long-duration open intervals reflect a structural fluctuation of the apo-protein that requires a Trp side chain at position  $\alpha$ 149. The structural elements that generate this spontaneous fluctuation include the protein, water, and extracellular ions (which are competitive inhibitors of the AChR transmitter binding site; Akk and Auerbach, 1996), perhaps in combination.



**Figure 7.** Mutations of  $\alpha$ W149 yield one-component open-interval duration histograms on nine different background constructs. All panels show an example histogram (arrows, long components) and cluster. (left) Background mutation alone. (right) With an  $\alpha$ W149 mutation. (A)  $\alpha$ -Subunit extracellular domain background mutations (DYP is  $\alpha$ D97A+ $\alpha$ Y127F+ $\alpha$ P272A; DYS is  $\alpha$ D97A+ $\alpha$ Y127F+ $\alpha$ S269I). (B)  $\delta$ -Subunit transmembrane domain (M2 helix) background mutations. In all cases, the  $\alpha$ W149 mutation eliminates the long open component (Fig 6, bottom).

## DISCUSSION

Fig. 2 C shows a close-up of the salient binding site residues in the 4-Å *Torpedo* AChR structure that possibly reflects an apo-R conformation (Unwin, 2005). There are no available AChR structures for liganded R or either liganded or apo-R\*. However, there are structures of the homologous ACh-binding protein (AChBP), with and without bound ligands (Fig. 2 D; Brejc et al., 2001; Celie et al., 2004). AChBP has an affinity for ACh that is approximately midway (on a log scale) between that of R and R\* in the AChR (Smit et al., 2001). Although this protein does not isomerize, a modified version of AChBP attached to the transmembrane domain of a 5-HT<sub>3A</sub> receptor has been reported to generate currents when exposed to ACh (Bouzat et al., 2004). There is some indication that AChBP resembles the liganded R\* conformation of AChRs (Brejc et al., 2001; Celie et al., 2004; Stewart et al., 2006).

We observe that in apo-AChRs, the binding site Trp residues ( $\alpha$ W149 and  $\epsilon$ W55/ $\delta$ W57) experience significant energy changes in R $\leftrightarrow$ R\* gating. The range energy change caused by mutation of either of these positions is substantially larger than that caused by mutation of each of the three Tyr residues. On a per-residue basis, the energy change of the two Trp residues is about twice that of the three Tyr residues. In unliganded gating, the repositioning of the two Trp residues is an energetically significant event that occurs at the onset of the channel-opening process. The three Tyr residues show smaller positional changes between apo-AChR and apo-AChBP compared with the two Trp residues, which may move from being separated into an edge to face alignment (Samanta et al., 1999; Guvench and Brooks, 2005; Mahalakshmi et al., 2005).

The binding site aromatic residues appear to act as a coherent unit in the gating conformational change, with  $\alpha$ W149 being an important main organizing element (Fig. 5 and Tables S3 and S4). With R substitutions, the energy changes at  $\alpha$ W149 are coupled with those of the three Tyr residues and the complementary Trp residue. The three Tyr residues interact more strongly with  $\alpha$ W149 than with each other or the complementary Trp. Also, the observation that the agonists  $\alpha$ W149,  $\alpha$ Y93, and  $\alpha$ Y190 experience their gating changes at approximately the same point along the reaction coordinate suggests that these entities move in a concerted manner between their R and R\* positions.  $\alpha$ Y198 has a lower  $\Phi$  value, but we do not understand the significance of this observation.

We are unable to identify the chemical forces that correlate with these changes in residue energy. In particular, the results presented here pertain to unliganded AChRs; that is, with water molecules and perhaps ions occupying the space that is occupied by agonists in diliganded gating. Certainly, the presence of ACh would be



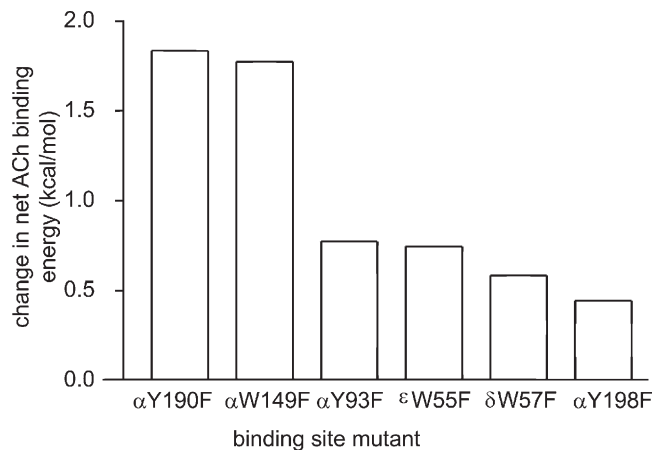
expected to significantly alter some aspects of the energy changes that we have measured. For example, the cation- $\pi$  interaction that is present between  $\alpha$ W149 and ACh (Gao et al., 1993; Zhong et al., 1998) would disappear in the apo-binding sites, and therefore we detect no preference of the R\* conformation for aromatic substitutions at any of the positions we have probed. However, the fact that the Trp residues of AChBP are in the edge to face alignment at both liganded and apo-structures (Fig. 2 D) supports the hypothesis that the general shape of the R\* transmitter binding site may be similar with and without bound agonists.

We can calculate the binding energy change experienced by ligands from the relationship  $K_d/J_d = \sqrt{(E_2/E_0)}$ . There are published estimates of  $E_2$  for AChR constructs (activated by ACh) having a Phe substitution at each aromatic position of the binding site (Chen et al., 1995; Akk et al., 1996, 1999; Akk, 2001, 2002; Bafna et al., 2009). As shown in Fig. 8 (also see Table S6), relative to the wt, the effect of a Phe substitution on the net binding energy (per site) was approximately threefold larger for positions  $\alpha$ Y190 and  $\alpha$ W149 ( $\sim 1.8$  kcal/mol) compared with positions  $\alpha$ Y93,  $\alpha$ Y198, and  $\delta/\epsilon$ W55/57 ( $\sim 0.6$  kcal/mol). The binding energy that drives gating appears to be derived mainly from interactions of ACh with  $\alpha$ W149 and  $\alpha$ Y190.

We now analyze in detail the consequences of one of these binding site mutations. The published  $E_2^{\text{ACh}}$  value for  $\alpha$ Y190F is 0.035. For this mutant,  $E_0 = 3.8 \times 10^{-7}$ , so we calculate  $K_d/J_d = \sim 303$  ( $\sim 22$  times lower than the wt). This single-atom perturbation reduces the per-site energy available for gating by ACh by 1.9 kcal/mol (from  $-5.2$  to  $-3.3$  kcal/mol). The published  $K_d^{\text{ACh}}$  value for  $\alpha$ Y190F is 5.2 mM, so we calculate  $J_d = \sim 17$   $\mu$ M. Relative to the wt, the  $\alpha$ Y190F mutant shows an  $\sim 800$ -fold reduction in  $E_2$  that can be traced to an  $\sim 1.7$ -fold reduction in  $E_0$ , an  $\sim 35$ -fold increase in  $K_d$ , and an 80-fold increase in  $J_d$ .

Our results suggest that the structural perturbation that gives rise to spontaneous, long-lived openings occurs at the transmitter binding site. This event probably involves  $\alpha$ W149 as well as other residues in all three binding site loops. Distant mutations did not affect the role of  $\alpha$ W149 in this regard, which suggests that the salient binding site perturbation is a localized event. Although more experiments are needed to further identify the physical basis of the long open component, our results do not support the hypothesis that brief versus long spontaneous openings reflect AChRs having one versus two C loops in a capped position (Mukhtasimova et al., 2009).

The pattern of the energy change at the unliganded AChR transmitter binding sites suggests that early and energetically significant events in the channel-opening cascade derive from conformational changes of the two Trp residues. Analyses of Phe mutations of the binding site aromatics suggest that  $\alpha$ Y190 (loop C) and  $\alpha$ W149



**Figure 8.** Effect of Phe substitutions on R versus R\* ACh binding energy. The y axis is the net change in the R versus R\* ACh binding free energy ( $= 0.59 \ln [(K_d/J_d)^{\text{mut}}/(K_d/J_d)^{\text{wt}}]$ ; Table S5). The mutations  $\alpha$ Y190F and  $\alpha$ W149F cause the biggest drop in the net binding energy.

(loop B) provide the bulk of the net R\* versus R ACh-binding energy. We hypothesize that the movements of these two residues are early events in the channel-opening conformational cascade. The unusual coupling of  $\alpha$ W149 (loop B) with  $\alpha$ Y93 (loop A) is noteworthy.

The  $E_0$  estimates for many different constructs open the possibility of engineering the AChR transmitter binding site. These values, along with  $E_2$  estimates, make it possible to calculate agonist-binding energy changes associated with gating and, thus, to identify the atomic forces between ligand, water, ions, and protein that promote the isomerization.

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