

pay-to-sudoku

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Live demo

- Live demos always fail without exception
 - Network will go offline
 - Laptop will start on fire
 - SHA256 collisions destroy Bitcoin network
 - Miners switch to dogecoin

Paying for the solution to a sudoku puzzle

- Alice wants the solution to a puzzle, **P**.

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Redeem script:

```
OP_???  
OP_???  
OP_???  
OP_???  
OP_???
```

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Redeem script:

```
OP_???  
OP_???  
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```

Problems

- The script (and the solution) could be gigantic for larger puzzles.
- Bitcoin's scripting system isn't expressive enough.
- Everyone else discovers the solution.
- If somebody tries to spend the script, someone else can spend it using their solution first.

Paying for the solution to a sudoku puzzle

- Alice wants to pay Bob to solve a puzzle.



```
OP_IF
  bob_pubkey
  OP_CHECKSIGVERIFY
  OP_SUDOKU...
OP_ELSE
  400000
  OP_CHECKLOCKTIMEVERIFY
  alice_pubkey
  OP_CHECKSIGVERIFY
OP_ENDIF
```

Problems

- The script (and the solution) could be gigantic for larger puzzles.
- Bitcoin's scripting system isn't expressive enough.
- Everyone else discovers the solution.
- ~~If somebody tries to spend the script, someone else can spend it using their solution first.~~

Zero-knowledge contingent payments

- Gregory Maxwell described them in 2011
- Relies on two processes:
 - An interactive zero-knowledge proving scheme
 - An atomic swap over the blockchain
- Achieves
 - Privacy of the solution (and the problem)
 - Small transaction size

HTLC (Hashed Timelock Contract)

Alice

SHA256(K)

Bob

K

HTLC (Hashed Timelock Contract)

Alice

Bob

SHA256(K)

K

```
OP_SHA256
h_key
OP_EQUAL
OP_IF
  bob_pubkey
  OP_CHECKSIG
OP_ELSE
  future_block_height
  OP_CHECKLOCKTIMEVERIFY
  OP_DROP
  alice_pubkey
  OP_CHECKSIGVERIFY
OP_ENDIF
```

HTLC (Hashed Timelock Contract)

Alice

Bob

SHA256(K)

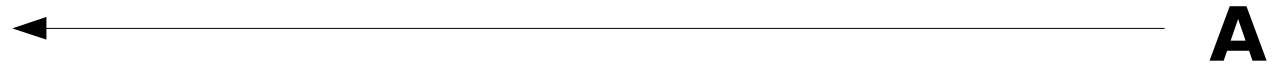
K

```
OP_SHA256
h_key
OP_EQUAL
OP_IF
  bob_pubkey
  OP_CHECKSIG
OP_ELSE
  future_block_height
  OP_CHECKLOCKTIMEVERIFY
  OP_DROP
  alice_pubkey
  OP_CHECKSIGVERIFY
OP_ENDIF
```

- Bob must disclose K to get the money
- Alice gets her money back if Bob doesn't provide K
- The transaction is not that big.

Alice

Bob



Alice

Bob



Alice

Bob

Q →

pk
vk →

A
K

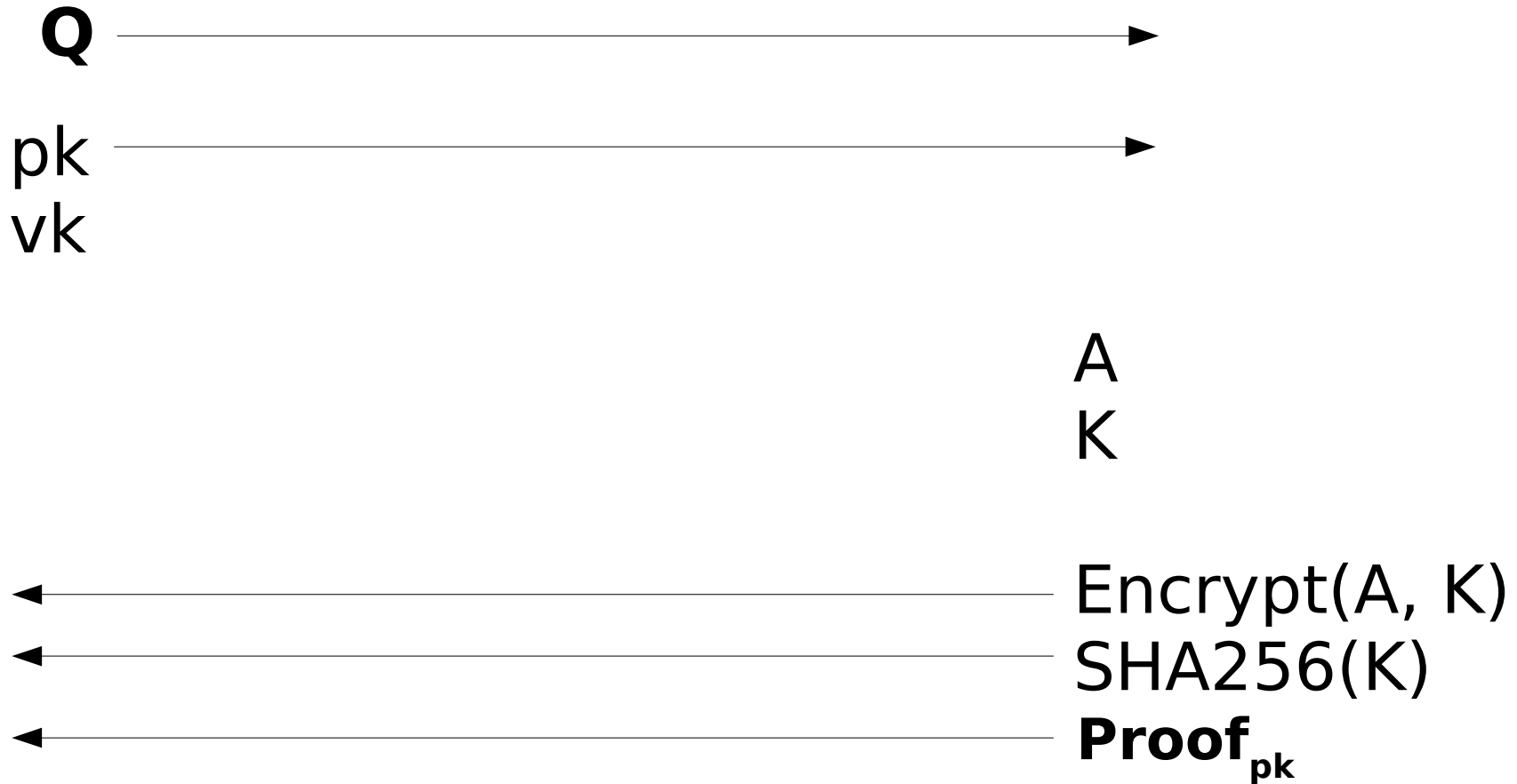
← Encrypt(A, K)
← SHA256(K)
← **Proof**_{pk}

Zero-knowledge proof

- Given a question **Q**, a hash **H**, and an encrypted answer **E**
- I know answer **A** and key **K**
- Such that
 - **A** answers **Q**
 - **E** is $\text{Encrypt}(\mathbf{A}, \mathbf{K})$
 - **H** is $\text{SHA256}(\mathbf{K})$

Alice

Bob



Alice uses a HTLC to pay Bob in exchange for **K**.
Alice decrypts with K to get the solution.

Pros and cons

- Pro: The transaction is *atomic, trustless,* and *private*.
- Pro: The transaction is small and completely prunable.
- Pro: We can do it on Bitcoin today!

Pros and cons

- Con: The transaction is interactive.
- Con: Constructing the zero-knowledge proof can take seconds to minutes depending on the complexity of the circuit.
- Con: The proving key can be tens to hundreds of megabytes in size depending on the complexity of the circuit.

Circuit Statistics

- 16x16 sudoku:
 - Proving key: **68MB**
 - Only needs to be computed once, so cost can be amortized.
 - Proving time: **10 to 20 seconds**
 - Proof: **288 bytes** (sent off chain)
 - Verification time: **40ms**
 - Circuit cost:
 - **Encrypt(A, K)** (81.86%)
 - ChaCha20 would be a 3x improvement over the current cipher.
 - **SHA256(K)** (10.23%)
 - Could use RIPEMD-160?
 - Solution validity (4.42%)
 - Mostly unoptimizable

Wrapping up

- Code:
<https://github.com/zcash/pay-to-sudoku>
- Thanks:
 - Gregory Maxwell
 - Pieter Wuille
 - Madars Virza
 - Andrew Poelstra
 - Zcash Company